

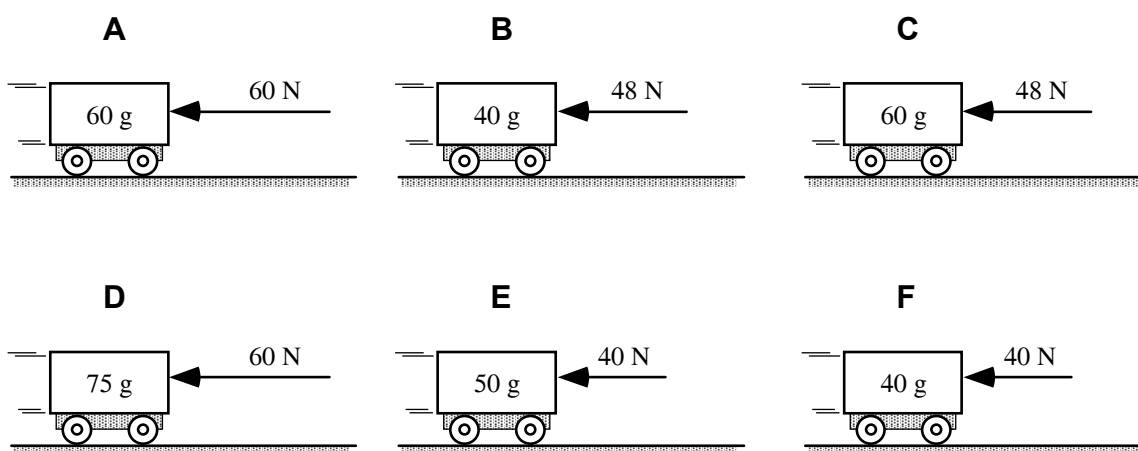
## Ranking Task Sample II

Each ranking task will have a number of situations, or variations of a situation, that have varying values for two or three variables. Your task is to rank these variations on a specified basis. After ranking the items, you will be asked to explain how you determined your ranking sequence and the reasoning behind the way you used the values of the variables to reach your answer. An example of how to work the ranking tasks follows.

### Example:

Shown below are six situations where a cart, which is initially moving to the right, has a force applied to it such that the force will cause the cart to come to a stop. All of the carts have the same initial speed, but the masses of the carts vary, as do the forces acting upon them.

Rank these situations, from greatest to least, on the basis of how long it will take each cart to stop.



Greatest 1 B 2 A 3 F 4 C 5 D 6 E Least

Or, all of these carts will require the same time to stop. \_\_\_\_\_

Please carefully explain your reasoning.

*I think the time depends on the acceleration, so I divided the forces by the masses.*

How sure were you of your ranking? (circle one)

Basically Guessed

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Sure

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Very Sure

9

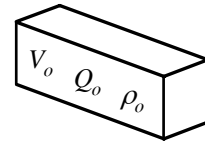
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Notice in this example that in one instance, two of the situations produced the same value of the ratio used to determine the ranking, and that the letters for the ones that tied are circled showing they were ranked equally (A and F). In another instance, three of the remaining situations have the same ranking and they are circled together (C and D and E), showing this result. In the same way, it is possible that all of the arrangements will give the same result for a particular basis. If that occurs, and only if that occurs, the option of all equal, or all the same, should be chosen.

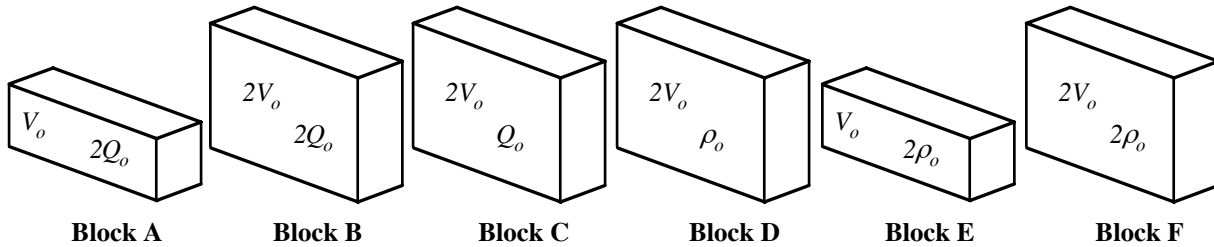
# **ELECTROSTATICS** **RANKING TASKS (RT)**

## **ET1-RT1: CHARGED INSULATING BLOCKS—CHARGE DENSITY**

The block of insulating material shown at right has a volume  $V_o$ . An overall charge  $Q_o$  is spread evenly throughout the volume of the block so that the block has a uniform charge density  $\rho_o$ .



Six additional charged insulating blocks are shown below. For each block, the volume is given as well as *either* the charge or the charge density.



**Rank the charge densities of the six blocks.**

Greatest 1 AEF 2 \_\_\_\_\_ 3 \_\_\_\_\_ 4 BD 5 \_\_\_\_\_ 6 C Least

OR, the charge density is the same for all six blocks. \_\_\_\_\_

OR, the ranking for the charge density cannot be determined. \_\_\_\_\_

**Carefully explain your reasoning.**

*Charge density is defined as the ratio of total charge divided by volume, so you compute that for each block if not already given.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

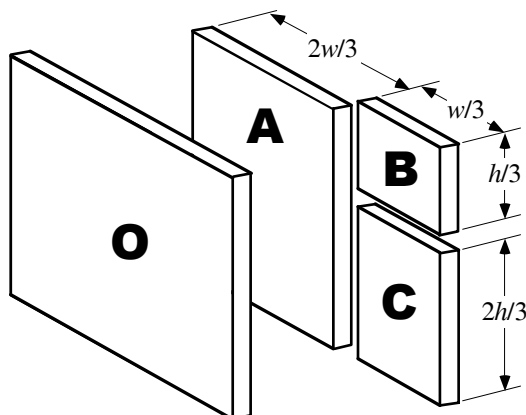
Sure

Very Sure

1      2      3      4      5      6      7      8      9      10

**ET1-RT2: BREAKING A CHARGED INSULATING BLOCK—CHARGE DENSITY**

A block of insulating material (labeled O in the diagram) with a width  $w$ , height  $h$ , and thickness  $t$  has a positive charge  $+Q_o$  distributed uniformly throughout its volume. The block is then broken into three pieces, A, B, and C, as shown.



**Rank the charge densities of the original block O, piece A, piece B, and piece C.**

Greatest 1 \_\_\_\_\_ 2 \_\_\_\_\_ 3 \_\_\_\_\_ 4 \_\_\_\_\_ Least

OR, the charge density is the same for all four pieces.   X  

OR, the ranking for the charge densities cannot be determined. \_\_\_\_\_

**Carefully explain your reasoning.**

*The charge density is not going to change because each block will have a charge proportional to its volume since the charge is uniformly distributed.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

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Sure

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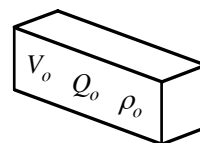
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Very Sure

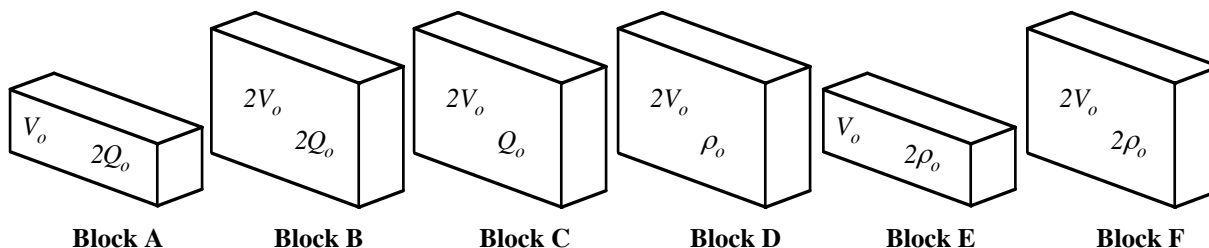
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### ET1-RT3: CHARGED INSULATING BLOCKS—CHARGE

The block of insulating material shown at right has a volume  $V_o$ . An overall charge  $Q_o$  is spread uniformly throughout the volume of the block so that the block has a charge density  $\rho_o$ .



Six additional charged insulating blocks are shown below. For each block, the volume is given as well as *either* the charge or the charge density of the block.



**Rank the overall charge of the six blocks.**

Greatest 1 F 2 ABDE 3 \_\_\_\_\_ 4 \_\_\_\_\_ 5 \_\_\_\_\_ 6 C Least

OR, the charge is the same for all six blocks. \_\_\_\_\_

OR, the ranking for the charge cannot be determined. \_\_\_\_\_

**Carefully explain your reasoning.**

*To determine the total charge for the blocks where it is not given we need to multiply the charge density by the volume and then rank the blocks.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

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Sure

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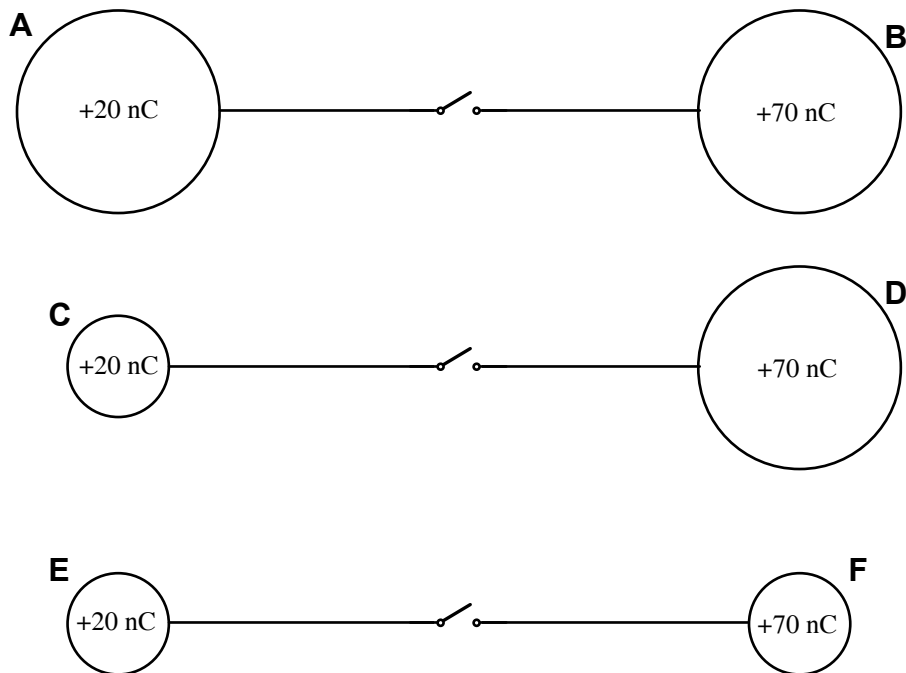
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Very Sure

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**ET1-RT4: PAIRS OF CONNECTED CHARGED CONDUCTORS—CHARGE**

Three pairs of charged, isolated, conducting spheres are connected with wires and switches. The spheres are very far apart. The large spheres have twice the radius of the small spheres. Each sphere on the left has a charge of  $+20\text{ nC}$  and each sphere on the right has a charge of  $+70\text{ nC}$  before the switches are closed.



**Rank the electric charge of the spheres after all of the switches are closed.**

Greatest 1 \_\_\_\_ **D** \_\_\_\_ 2 \_\_\_\_ **ABEF** \_\_\_\_ 3 \_\_\_\_ 4 \_\_\_\_ 5 \_\_\_\_ 6 \_\_\_\_ **C** \_\_\_\_ Least

OR, the electric charge is the same for all six spheres. \_\_\_\_

OR, the ranking of the electric charge cannot be determined. \_\_\_\_

**Carefully explain your reasoning.**

*The charges will move until the potential of each sphere will be the same. Equal size spheres will share the charge equally, but where the sizes differ the larger sphere will have the larger charge.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

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Sure

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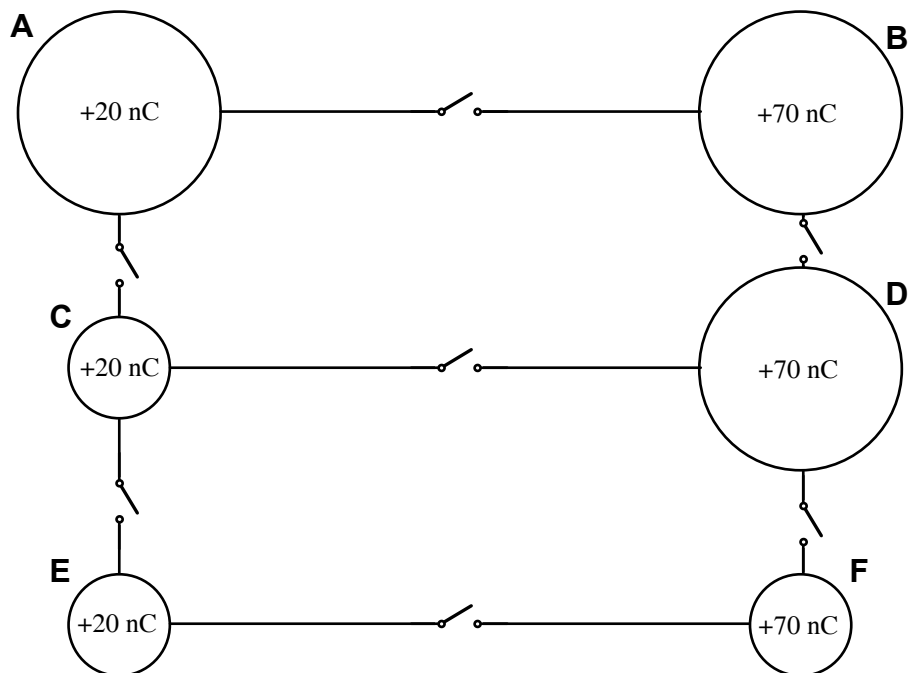
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Very Sure

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**ET1-RT5: COLLECTION OF SIX CHARGED CONNECTED CONDUCTORS—CHARGE**

Six charged conducting spheres are connected with wires and switches. The large spheres have twice the radius of the small spheres. Each sphere on the left has a charge of  $+20\text{ nC}$  and each sphere on the right has a charge of  $+70\text{ nC}$  before the switches are closed.



**Rank the electric charge of the spheres after all of the switches are closed.**

Greatest 1 ABD 2 \_\_\_\_\_ 3 \_\_\_\_\_ 4 CEF 5 \_\_\_\_\_ 6 \_\_\_\_\_ Least

OR, the electric charge is the same for all six spheres. \_\_\_\_\_

OR, the ranking of the electric charge cannot be determined. \_\_\_\_\_

**Carefully explain your reasoning.**

*The charges will move until the potential of each sphere is the same, so the larger spheres will all have the same charge, as will the three smaller spheres.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

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Sure

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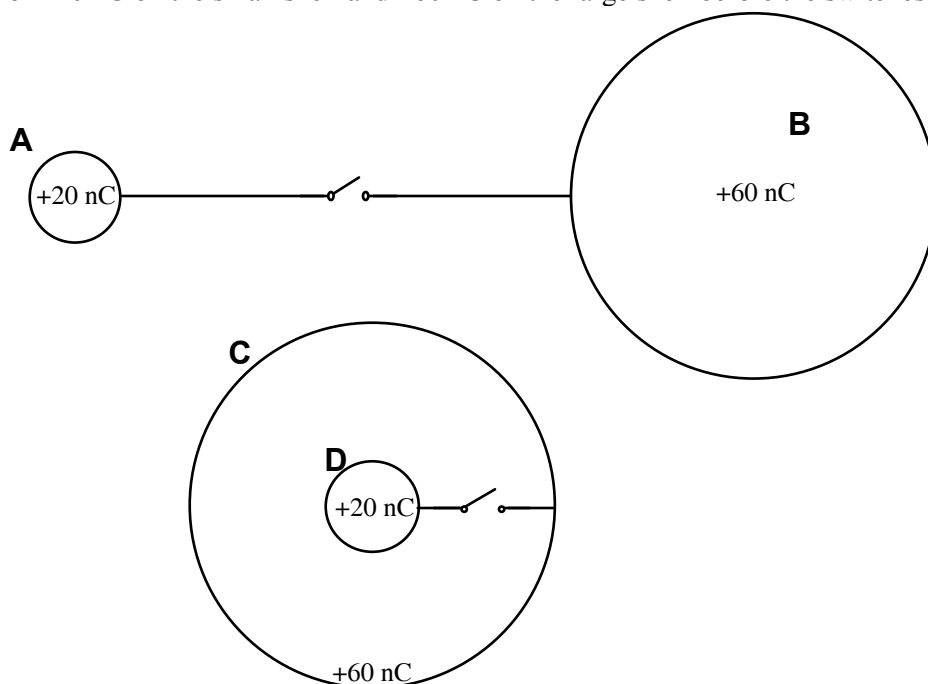
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Very Sure

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**ET1-RT6: PAIRS OF OUTSIDE AND INSIDE CONNECTED CHARGED CONDUCTORS—CHARGE**

Two pairs of charged, hollow, spherical conducting shells are connected with wires and switches. The system AB is very far from CD. The large shells have four times the radius of the small shells. Each pair has a charge of  $+20\text{ nC}$  on the small shell and  $+60\text{ nC}$  on the large shell before the switches are closed.



**Rank the electric charge on the shells A-D after the switches are closed.**

Greatest 1   C   2   B   3   A   4   D   Least

OR, the electric charge is the same for all four shells. \_\_\_\_\_

OR, the ranking of the electric charge cannot be determined. \_\_\_\_\_

**Carefully explain your reasoning.**

*The charge flows until the potential is the same of each sphere for A and B but all the charge on D flows to the outside sphere since there is no charge inside a conducting object giving C the largest charge.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

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Sure

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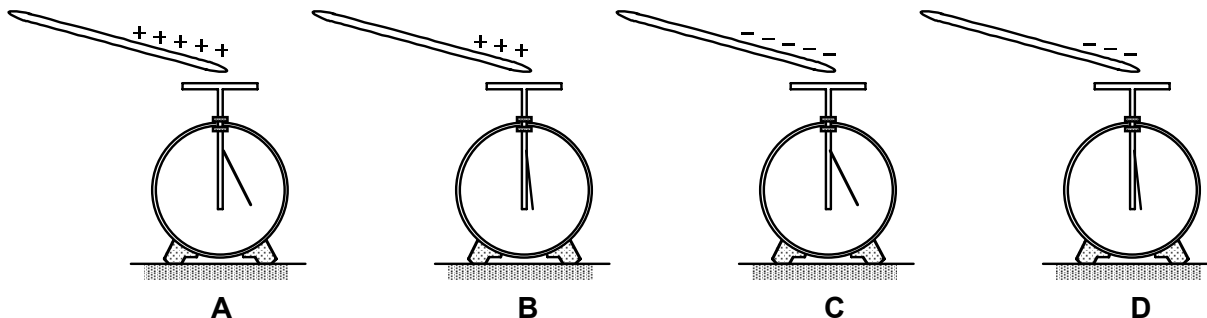
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Very Sure

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### ET1-RT7: CHARGED ROD AND ELECTROSCOPE—EXCESS CHARGE

In each of the four cases below, a charged rod is brought close to an electroscope that is initially uncharged. In cases A and B, the rod is positively charged; in cases C and D, the rod is negatively charged. In cases A and C, the leaf of the electroscope is deflected the same amount, which is more than it is deflected in cases B and D.



**Rank the net charge on the electroscope while the charged rod is near.** (This will be a negative value if there is more negative than positive charge on the electroscope.)

Greatest positive 1 \_\_\_\_\_ 2 \_\_\_\_\_ 3 \_\_\_\_\_ 4 \_\_\_\_\_ Greatest negative

OR, the net charge is the same for all four situations but it is not zero. \_\_\_\_\_

OR, the net charge is zero for all of these situations.   X  

OR, the ranking for the net charge cannot be determined from the information given. \_\_\_\_\_

**Carefully explain your reasoning.**

*The net charge on the electroscope, assuming the rod does not touch it, is zero in all four cases since no charge is transferred.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

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Sure

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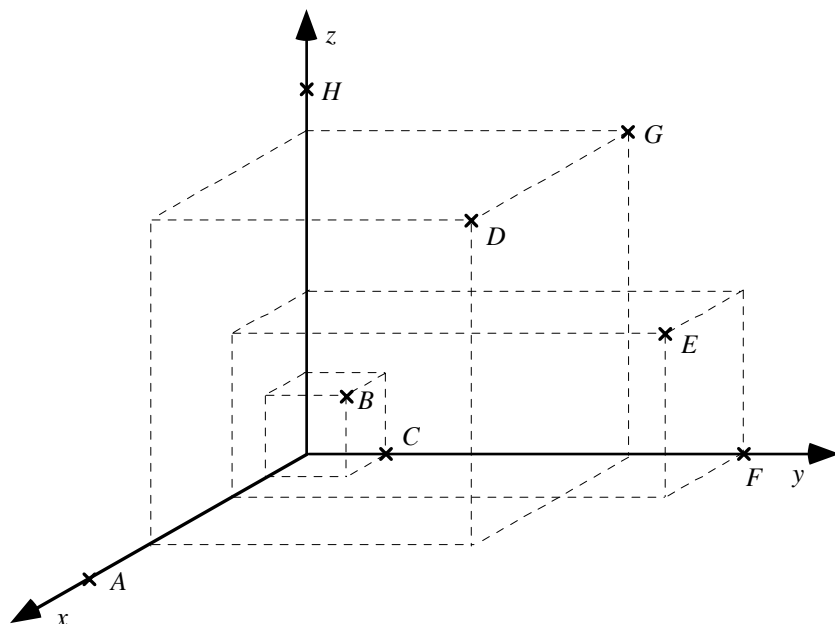
Very Sure

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**ET3-RT1: THREE-DIMENSIONAL LOCATIONS IN A CONSTANT ELECTRIC POTENTIAL—FORCE**

The electric potential has a constant value of six volts everywhere in a three-dimensional region, part of which is shown below.



**Rank the strength (magnitude) of the electric force on a charge of  $+2\ \mu\text{C}$  if it is placed at the labeled points.**

Greatest 1 \_\_\_\_\_ 2 \_\_\_\_\_ 3 \_\_\_\_\_ 4 \_\_\_\_\_ 5 \_\_\_\_\_ 6 \_\_\_\_\_ 7 \_\_\_\_\_ 8 \_\_\_\_\_ Least

OR, the electric force is the same but not zero for all of these points. \_\_\_\_\_

OR, the electric force is zero for all of these points.   X  

OR, the ranking for the electric force cannot be determined for all of these points. \_\_\_\_\_

**Carefully explain your reasoning.**

*The field is zero since the potential does not change, thus the force is zero.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

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Sure

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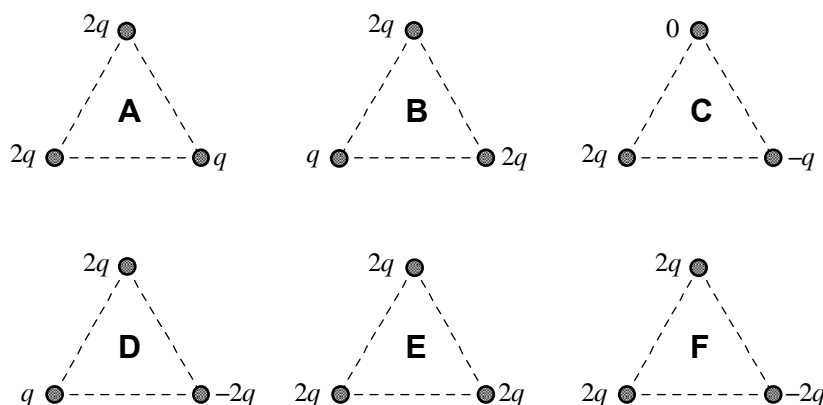
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Very Sure

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### ET3-RT2: CHARGES ARRANGED IN A TRIANGLE—FORCE

In each case below, three particles are fixed in place at the vertices of an equilateral triangle. The triangles are all the same size. The particles are charged as shown. (In case C, the top particle has no charge.)



Rank the magnitude of the net electric force on the lower left particle.

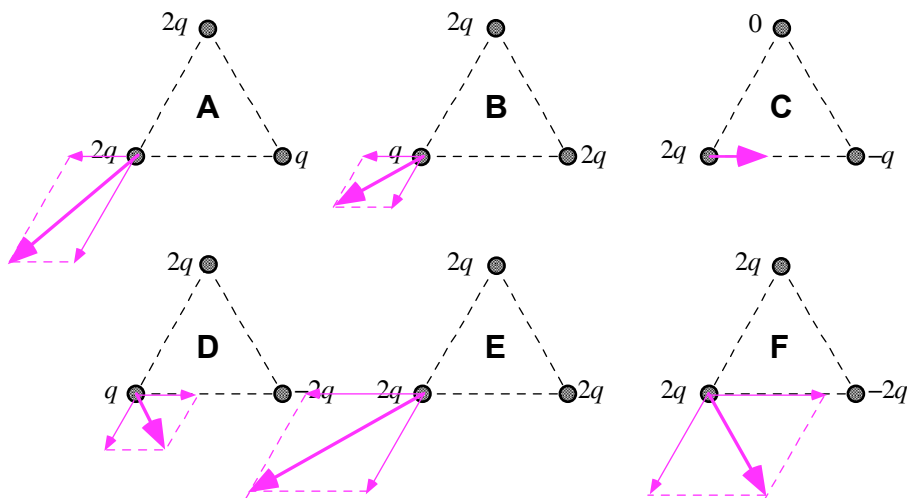
Greatest 1 E 2 A 3 F 4 B 5 CD 6 \_\_\_\_\_ Least

OR, the net electric force on the lower left particle is the same for all six cases. \_\_\_\_\_

OR, the ranking for the net electric force on the lower left particle cannot be determined. \_\_\_\_\_

Carefully explain your reasoning.

*We apply Coulomb's Law to the interaction between the lower left charge and the other two, taking account of the vector process of adding the forces.*



How sure were you of your ranking? (circle one)

Basically Guessed

1

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Sure

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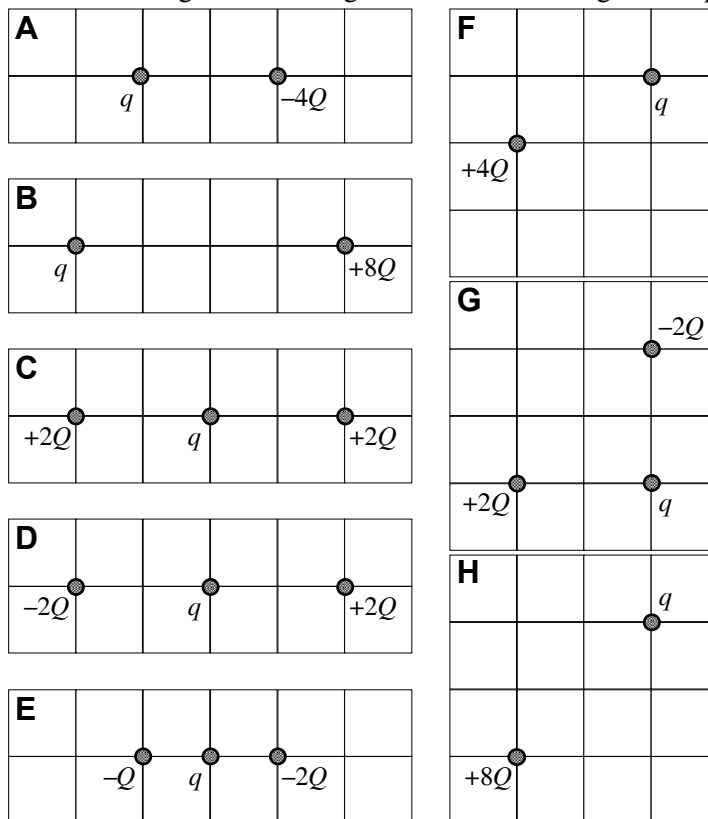
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Very Sure

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### ET3-RT3: CHARGES IN A PLANE—FORCE

In each case shown below, small charged particles are fixed on grids having the same spacing. Each charge  $q$  is identical, and all other charges have a magnitude that is an integer multiple of  $Q$ .



Rank the magnitude of the electric force on the charge labeled  $q$  due to the other charges.

Greatest 1 ADEH 2 \_\_\_\_\_ 3 \_\_\_\_\_ 4 \_\_\_\_\_ 5 F 6 G 7 B 8 C Least

OR, the electric force on  $q$  is the same but not zero for all eight cases. \_\_\_\_\_

OR, the electric force on  $q$  is zero for all eight cases. \_\_\_\_\_

OR, the ranking for the electric force on  $q$  cannot be determined. \_\_\_\_\_

Carefully explain your reasoning.

*Apply Coulomb's Law to the interaction between each charge and  $q$  and then perform the vector sum when more than one charge is involved.*

How sure were you of your ranking? (circle one)

Basically Guessed

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Sure

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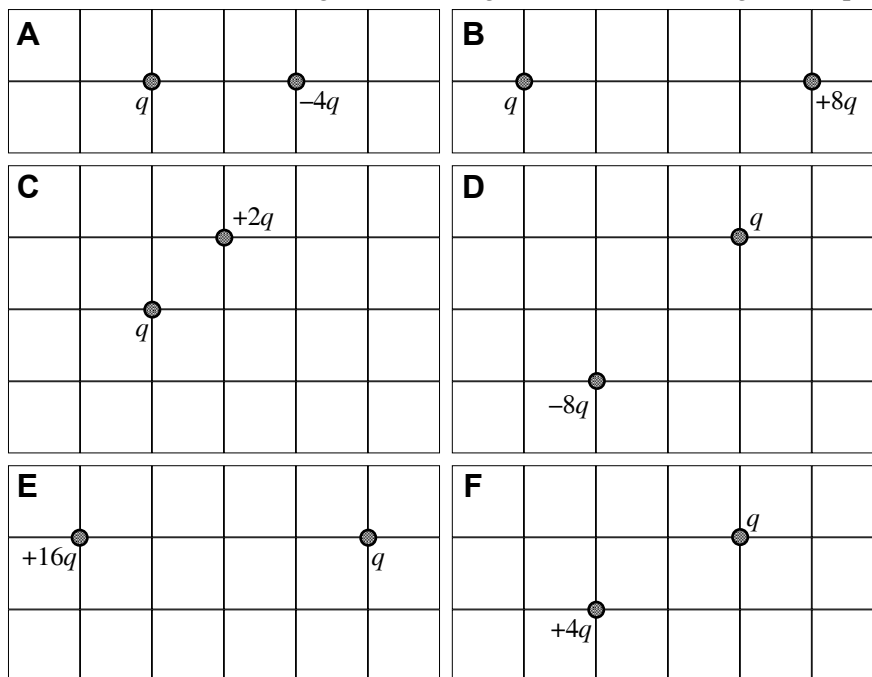
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Very Sure

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### ET3-RT4: TWO CHARGES—FORCE

In each case shown below, small charged particles are fixed on grids having the same spacing. Each charge  $q$  is identical, and all the other charges have a magnitude that is an integer multiple of  $q$ .



Rank the magnitude of the electric force on the charge labeled  $q$  due to the other charge.

Greatest 1 ACDE 2 \_\_\_\_\_ 3 \_\_\_\_\_ 4 \_\_\_\_\_ 5 F 6 B Least

OR, the electric force on  $q$  is the same but not zero for all six cases. \_\_\_\_\_

OR, the electric force on  $q$  is zero for all six cases. \_\_\_\_\_

OR, the ranking for the electric force on  $q$  cannot be determined. \_\_\_\_\_

Carefully explain your reasoning.

*The force (Coulomb's Law) is proportional to the product of the charges and inversely proportional to the square of the distance between them. The larger charges and the closer charges are ranked higher.*

How sure were you of your ranking? (circle one)

Basically Guessed

Sure

Very Sure

1

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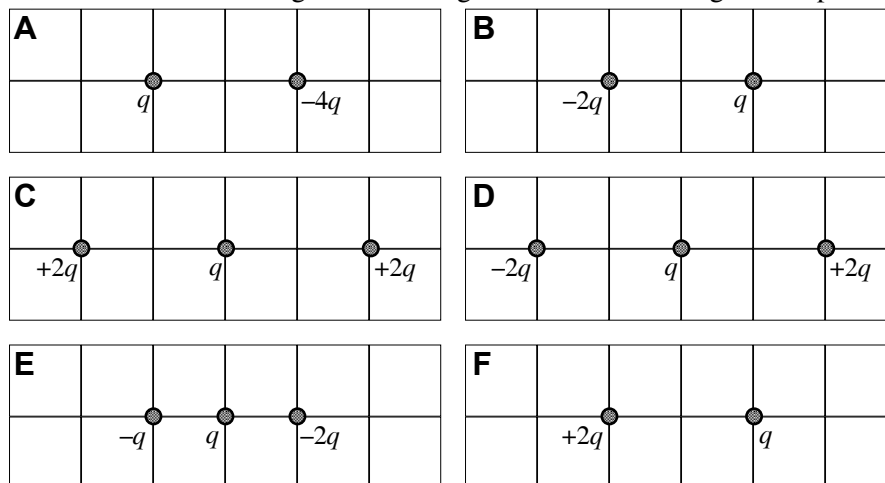
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### ET3-RT5: TWO AND THREE CHARGES IN A LINE—FORCE

In each case shown below, small charged particles are fixed on grids having the same spacing. Each charge  $q$  is identical, and all the other charges have a magnitude that is an integer multiple of  $q$ .



Rank the magnitude of the electric force on the charge labeled  $q$  due to the other charges.

Greatest 1 ADE 2 \_\_\_\_\_ 3 \_\_\_\_\_ 4 BF 5 \_\_\_\_\_ 6 C Least

OR, the electric force on  $q$  is the same but not zero for all six cases. \_\_\_\_\_

OR, the electric force on  $q$  is zero for all six cases. \_\_\_\_\_

OR, the ranking for the electric force on  $q$  cannot be determined. \_\_\_\_\_

Carefully explain your reasoning.

*In cases A, B and F the net force on  $q$  is found simply using Coulomb's Law. In C, D and E, use Coulomb's law to find the magnitude of the forces on  $q$  by each of the other two charges. Then, taking into consideration the direction of these forces, add them vectorially to find the magnitude of the net force on  $q$ .*

How sure were you of your ranking? (circle one)

Basically Guessed

1

2

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Sure

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Very Sure

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### ET3-RT6: CHARGED RODS AND POINT CHARGES—FORCE

In each case A-D, a point charge  $+q$  is fixed in place as well as some other point charges or charged rods.

The charged insulating rod in case A has a length  $x$  and a charge  $+2Q$  distributed uniformly along it. The charged insulating rod in case D is an arc of radius  $y$ , and has a charge  $+2Q$  distributed uniformly along it.

**Rank the magnitude of the electric force on  $+q$  due to the other charges in each case.**

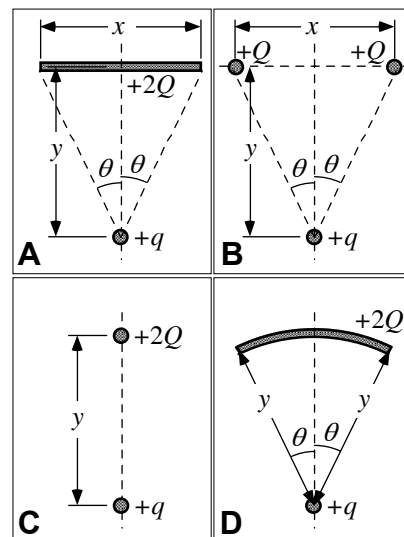
Greatest 1 C 2 D 3 A 4 B Least

OR, the electric force on  $+q$  is the same for all four cases. \_\_\_\_\_

OR, the ranking for the electric force on  $+q$  cannot be determined. \_\_\_\_\_

**Carefully explain your reasoning.**

*C has greatest force since total charge  $2Q$  is concentrated in one spot at distance  $y$ . B is least since charge is split in half and each half is farther away and greatest angle. A and D are both smaller than C since the charge is spread out, but larger than B since more of the charge is closer to  $q$  and closer to being on the same vertical line. D is greater than A since the charge in D is never farther than the distance  $y$ , whereas in A, the charge at the ends of the line is farther away than  $y$ .*



**How sure were you of your ranking? (circle one)**

Basically Guessed

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Sure

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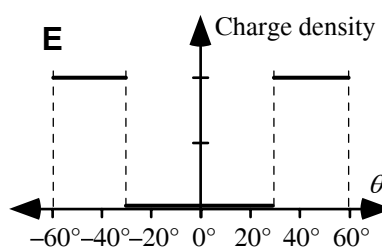
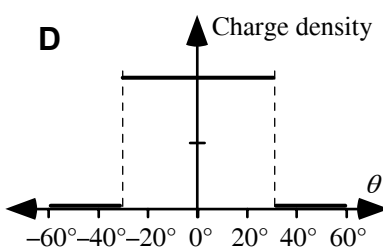
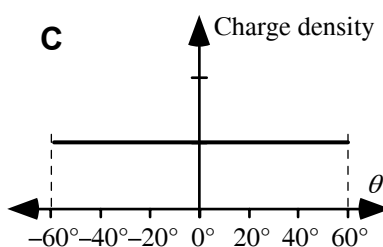
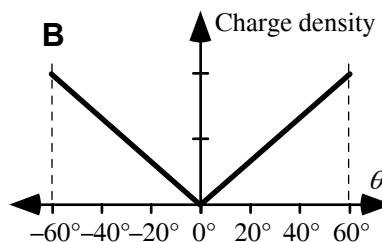
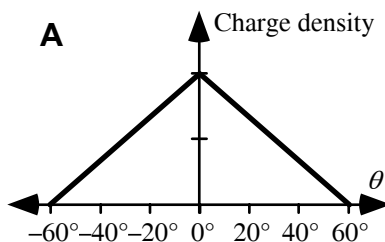
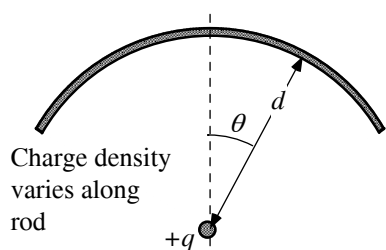
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Very Sure

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### ET3-RT7: CHARGED CURVED ROD—FORCE

A point charge  $+q$  is placed near a curved, charged, insulating rod as shown at left below. The charge is placed at the center of curvature of the curved rod. For each of the five cases A-E, the charge density on the rod varies according to the graphs, but the total charge is the same.



Rank the magnitude of the electric force on  $+q$  due to the charge in the curved rod in each case.

Greatest 1 D 2 A 3 C 4 B 5 E Least

OR, the electric force on  $+q$  is the same (but not zero) for all five cases. \_\_\_\_

OR, the electric force on  $+q$  is zero for all five cases. \_\_\_\_

OR, the ranking for the electric force on  $+q$  cannot be determined. \_\_\_\_

Carefully explain your reasoning.

*Vector addition or integration yields that more concentrated charge distribution gives larger force since the x-components cancel due to symmetry. The largest will be the one where the y-components are larger. This will occur when the charge is concentrated near  $\theta=0$ .*

How sure were you of your ranking? (circle one)

Basically Guessed

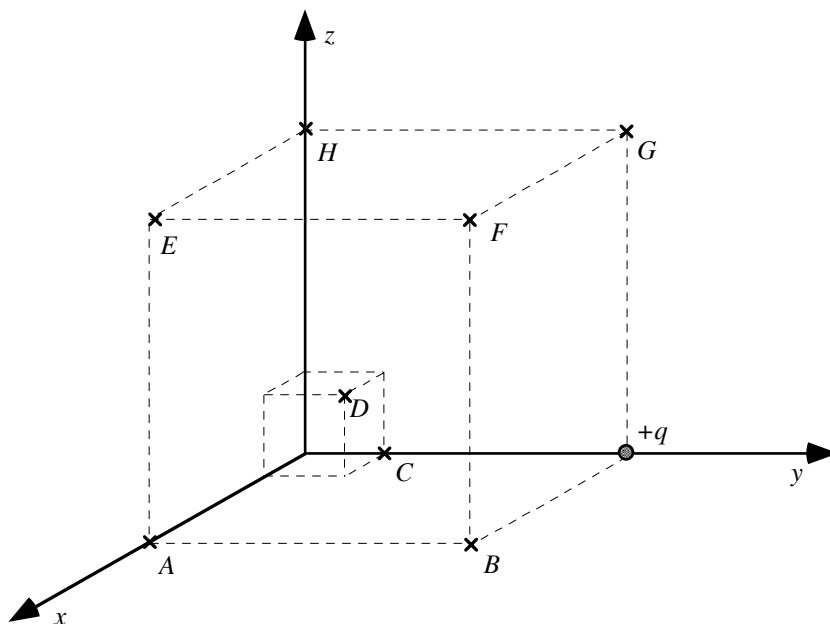
Sure

Very Sure

1 2 3 4 5 6 7 8 9 10

**ET3-RT8: THREE-DIMENSIONAL LOCATIONS NEAR A POINT CHARGE—ELECTRIC FORCE**

There is a positive point charge  $+q$  located at  $(0, 3, 0)$  as shown in the three-dimensional region below. Within that region are points located on the corners of two cubes as shown below. The small cube has edges of 1 centimeter length and the larger cube has edges of 3 centimeter length.



Rank the strength (magnitude) of the electric force on a  $+3q$  point charge if it is placed at the labeled points.

Greatest 1 C 2 D 3 BG 4 \_\_\_\_\_ 5 AFH 6 \_\_\_\_\_ 7 \_\_\_\_\_ 8 E Least

OR, the electric force is the same but not zero for all these points. \_\_\_\_\_

OR, the electric force is zero for all these points. \_\_\_\_\_

OR, the ranking for the electric force cannot be determined for all these points. \_\_\_\_\_

**Carefully explain your reasoning.**

*The force between two point charges decreases as the distance between those charges increases.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

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Sure

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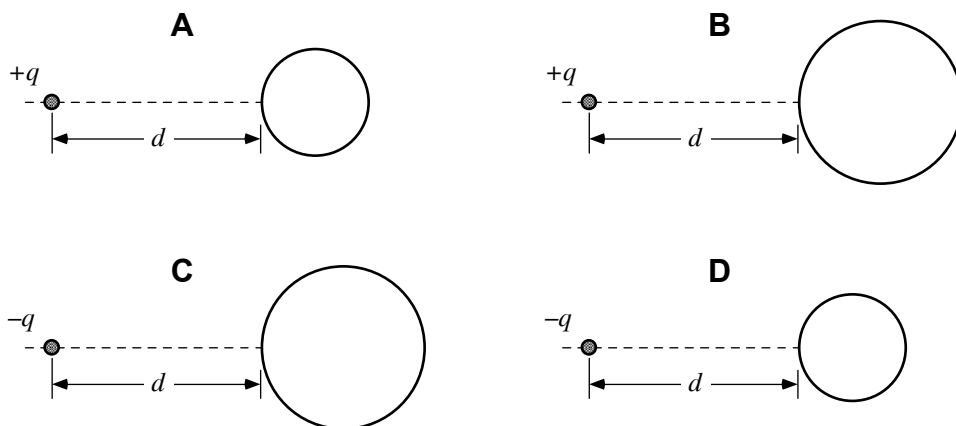
Very Sure

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### ET3-RT9: SPHERE AND A POINT CHARGE—FORCE

A point charge is placed a distance  $d$  away from a neutral metal sphere. The diameters of the spheres in A and D are the same and smaller than the equal diameters in B and C. The point charge is positive for cases A and B, and negative for C and D.



**Rank the force exerted on the point charge by the sphere** (let a force to the right be a positive force and a force to the left be a negative force).

Greatest positive 1 BC 2 \_\_\_\_\_ 3 AD 4 \_\_\_\_\_ Greatest negative

OR, the force is the same but not zero for all four situations. \_\_\_\_\_

OR, the force is zero for all these situations. \_\_\_\_\_

OR, the ranking for the forces cannot be determined. \_\_\_\_\_

**Carefully explain your reasoning.**

*The point charges in all these cases induce a charge distribution on the metal sphere that causes them to attract each other since the charge induced on the side of the sphere closest is opposite the sign of the point charge. These attract while the charge on the side farthest will have the same sign of the point charge, which will cause a repelling force. Since in each case the charge is the same distance from the sphere, the effect of the farthest side will determine the ranking. B and C have the largest net force because the spheres are larger and thus the repulsion force is smaller.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

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Sure

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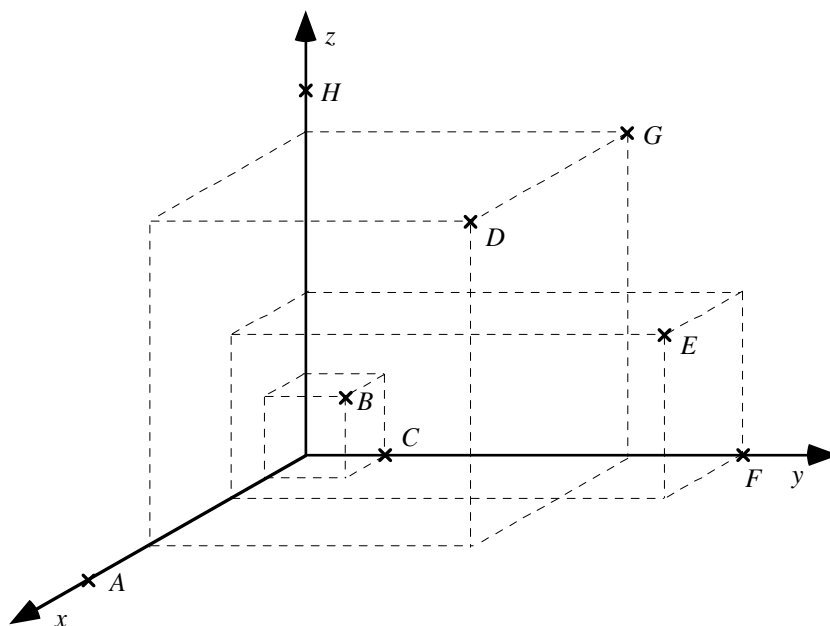
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Very Sure

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**ET3-RT10: THREE-DIMENSIONAL LOCATIONS IN A UNIFORM ELECTRIC FIELD—ELECTRIC FORCE**

All the labeled points are within a region of space with a uniform electric field. The electric field points toward the top of the page (that is, in the positive  $z$ -direction).



**Rank the magnitude of the electric force on a charge of  $+2 \mu\text{C}$  at the labeled points.**

Greatest 1 \_\_\_\_\_ 2 \_\_\_\_\_ 3 \_\_\_\_\_ 4 \_\_\_\_\_ 5 \_\_\_\_\_ 6 \_\_\_\_\_ 7 \_\_\_\_\_ 8 \_\_\_\_\_ Least

OR, the electric force is the same but not zero for all of these points.   X  

OR, the electric force is zero for all of these points. \_\_\_\_\_

OR, the ranking for the electric force cannot be determined for all of these points. \_\_\_\_\_

**Carefully explain your reasoning.**

*Since the field is the same at all these points and  $F=qE$ , the electric force will also be the same for the charge.*

**How sure were you of your ranking? (circle one)**

Basically Guessed

Sure

Very Sure

1

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