Econometric Analysis 8th Edition Greene Solutions Manual

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Chapter 1

Econometrics

There are no exercises or applications in Chapter 1.



(Dates were added to the figure by editing.)

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Chapter 2

The Linear Regression Model

There are no exercises or applications in Chapter 2.

Example 2.1. Keynes's Consumption import\$ Year х С W

plot;lhs=x;rhs=c;limits=200,350; endpoints=225,375;regression
;title=Figure 2.1 Consumption Data, 1940-1950 \$



(Dates and dashed lines were added by editing.)



Example 2.7. Nonzero Conditional Mean of the Disturbances

Chapter 3

Least Squares Regression

EXAMPLES – Section 3.2.2 and Table 3.2 Import\$

TWDOLCÓ								
YEAR RealG	NP Invest	GNPDefl	Interest	Infl	Trend	RealInv		
2000 87.	1 2.034	81.9	9.23	3.4	1	2.484		
2001 88.	0 1.929	83.8	6.91	1.6	2	2.311		
2002 89.	5 1.925	85.0	4.67	2.4	3	2.265		
2003 92.	0 2.028	86.7	4.12	1.9	4	2.339		
2004 95.	5 2.277	89.1	4.34	3.3	5	2.556		
2005 98.	7 2.527	91.9	6.19	3.4	6	2.750		
2006 101.	4 2.681	94.8	7.96	2.5	7	2.828		
2007 103.	2 2.644	97.3	8.05	4.1	8	2.717		
2008 102.	9 2.425	99.2	5.09	0.1	9	2.445		
2009 100.	0 1.878	100.0	3.25	2.7	10	1.878		
2010 102.	5 2.101	101.2	3.25	1.5	11	2.076		
2011 104.	2 2.240	103.3	3.25	3.0	12	2.168		
2012 105.	6 2.479	105.2	3.25	1.7	13	2.356		
2013 109.	0 2.648	106.7	3.25	1.5	14	2.482		
2014 111.	6 2.856	108.3	3.25	0.8	15	2.637		
EndData								
Create ; Y	= RealIn	v \$						
Create ; T	= trend	s .						
Create ; G	= realon	ь s						
Create : R	= intere	st Ś						
Create : P	= infl \$							
Namelist:z	=v.t.g.r.p	Ś						
Detat · r	1/0/9/2/P	т						
		S	tandard					Missing
Variablel	Me	an De	viation	Min	imum	Maximum	Cases	Values
+-								
YI	2.4200	67	.262666	1	. 878	2.828	15	0
TI	8	.0 4	.472136		1.0	15.0	15	0
GI	99.413	33 7	.525468		87.1	111.6	15	0
RI	5.0706	67 2	.081351		3.25	9.23	15	0
PI	2.3	26 1	.092703		.1	4.1	15	0
+-								
Descriptiv	e Statisti	cs for	5 variab	les				
Dstat resu	lts are ma	trix LAS	TDSTA in	current	projec	t.		
Regress;Lh	s=v;rhs=on	e,t,a,r,	o\$		F==]==			
Ordinary	least s	quares r	egression					
LHS=Y	Mean	-	=	2	. 42007			
	Standar	d deviat	ion =	_	26267			
	No. of	observat	ions =		15	DegFreedom	Mean	square
Regression	Sum of	Squares	=		760908	209110000m		19023
Residual	Sum of	Squares	=	•	205002	10		02050
Total	Sum of	Squares	_	•	965911	14		06899
10tai	Standar	d orror	of o -	•	1/310	Doot MSE		11601
₽i+	Besmar	a error (- 51 6		79776	P-bar source	bo	70297
Model test	EL V	101	_	٩	27026	Prob E > Et	-eu	00213
	FL 4,			9 	. 2 / 920	FIOD F / F'		
+		-	tandard		Droh	معد معد المعد ا معد المعد ا	onfidor	~~~~
vi Vi	Coefficio	nt S	Error	+	1+1>7	/. 90°C '* T≁	torval	
۱ × ۱ - ×				د 				
Constant	-6.26176	***	1.93671	-3.23	.0090	-10.57700) -1.94	651

T	16187***	.04739	-3.42	.0066	26746	05628
G	.09960***	.02421	4.11	.0021	.04566	.15355
R	.01972	.03380	.58	.5725	05559	.09503
P	01109	.03990	28	.7867	09998	.07781
***, **,	* ==> Significanc	e at 1%, 5%	, 10% l	evel.		
Model was	s estimated on Aug	01, 2017 at	08:37:	09 AM		
Namelist; Matrix ;	; x=one,t,g,r,p\$; list;x'x\$					
RESULT	+ 1	2		3	4	5
1	+ 1 15.0000	120.000	1	491.20	76.0600	33.9000
2	120.000	1240.00	1	2381.5	522.060	244.100
3	1491.20	12381.5	1	49038.	7453.03	3332.83
4	76.0600	522.060	7	453.03	446.323	186.656
5	33.9000	244.100	3	332.83	186.656	93.3300
Matrix ;	list;x'y\$					
	+					
RESULT	1					
1	36.3010					
2	288.691					
3	3612.90					
4	188.300					
5	82.8193					
Matrix ;	list; <x'x>*x'y\$</x'x>					
RESULT	+ 1					
	+					
1						
2						
3						
4	1 - 0110883					
5	.0110005					
Matrix ;	list;xcor(z)\$ +					
Cor.Mat.	Y Т +	G	R	P		
Y	1.0000010441	.14809	.55261	.19388		
т	10441 1.00000	.95910 -	.66317	39612		
G	.14809 .95910	1.00000 -	.49410	32384		
R	.5526166317	49410 1	.00000	.46358		
P	.1938839612	32384	.46358	1.00000		
Create ;	dy = dev(y) \$					
Create ;	dt = dev(t) \$					
Create ;	dg = dev(g) \$					
Calc ; li	ist ; xbr(y)					
; xł	br(t)					
; xł	br(g) \$					
[CALC]	= 2.4	200667				
[CALC]	= 8.0	000000				
[CALC]	= 99.4	133333				
Calculato	or: Computed 3 sc	alar result	s			
Calc ; li	ist ; sty = dt'dy					
; so	gg = dg'dg					
; so	gy = dg'dy					
; st	tg = dt'dg					
; st	tt = dt'dt\$	170000				
[CALC] ST	$r_{1} = -1.7$	T 10000				
[CALC] SC	JG = /92.8	51333				

```
[CALC] SGY = 4.0982867
[CALC] STG = 451.9000000
[CALC] STT = 280.0000000
Calculator: Computed 5 scalar results
Calc ; list ; b2 = (sty*sgg - sgy*stg)/(stt*sgg-stg*stg)$
[CALC] B2 =
                -.1806630
Calc ; list ; b3 = (sgy*stt - sty*stg)/(stt*sgg-stg*stg)$
                .1081404
[CALC] B3 =
Calc ; list ; b1 = xbr(y) - b2*xbr(t)-b3*xbr(g)$
[CALC] B1
           = -6.8852242
Calc ; list ; byg = sgy / sgg $
[CALC] BYG =
                      .0051690
Calc ; list ; byt = sty / stt $
[CALC] BYT = -.0061321
Calc ; list ; btg = stg / sgg$
[CALC] BTG =
                      .5699638
Calc ; list ; r2gt=stg^2/(sgg*stt)$
[CALC] R2GT = .9198809
Calc ; list ; byg_t=byg-((byt*btg-r2gt*byg)/(1-r2gt))$
[CALC] BYG T =
                   .1081404
Namelist ; yvar=y $
Matrix;list;xcor(x,yvar)$
-----
         Y
Cor.Mat.|
------
    ONE | .00000
      T| -.10441
      G| .14809
      R| .55261
      P| .19388
Regress; quietly ; Lhs=y; rhs=one, t, g, r, p$
Matrix ; vars = diag(varb) ; sdevs=sqrt(vars)$
Matrix ; tstats = <sdevs>*b$
Matrix ; pcor = dirp(tstats,tstats) + degfrdm$
Matrix ; pci = diri(pcor)$
Matrix ; pcor = dirp(tstats,tstats,pci)$
Matrix ; list ; pcor = esqr(pcor)$
PCOR |
                  1
-----
             .000000
      1|
              .733814
      21
             .792847
      31
             .181449
      4 |
      5| .0875491
```

Exercises

1. Let
$$\mathbf{X} = \begin{bmatrix} 1 & x_1 \\ \dots & \dots \\ 1 & x_n \end{bmatrix}$$
.

or

(a) The normal equations are given by (3-12), $\mathbf{X}' \mathbf{e} = \mathbf{0}$ (we drop the minus sign), hence for each of the columns of \mathbf{X} , \mathbf{x}_k , we know that $\mathbf{x}_k' \mathbf{e} = 0$. This implies that $\sum_{i=1}^n e_i = 0$ and $\sum_{i=1}^n x_i e_i = 0$.

(b) Use $\sum_{i=1}^{n} e_i$ to conclude from the first normal equation that $a = \overline{y} - b\overline{x}$.

(c) We know that $\sum_{i=1}^{n} e_i = 0$ and $\sum_{i=1}^{n} x_i e_i = 0$. It follows then that $\sum_{i=1}^{n} (x_i - \overline{x}) e_i = 0$ because

 $\sum_{i=1}^{n} \overline{x} e_i = \overline{x} \sum_{i=1}^{n} e_i = 0$. Substitute e_i to obtain $\sum_{i=1}^{n} (x_i - \overline{x})(y_i - a - bx_i) = 0$

or $\sum_{i=1}^{n} (x_i - \overline{x})(y_i - \overline{y} - b(x_i - \overline{x})) = 0$

Then, $\sum_{i=1}^{n} (x_i - \overline{x})(y_i - \overline{y}) = b \sum_{i=1}^{n} (x_i - \overline{x})(x_i - \overline{x}))$ so $b = \frac{\sum_{i=1}^{n} (x_i - \overline{x})(y_i - \overline{y})}{\sum_{i=1}^{n} (x_i - \overline{x})^2}$.

(d) The first derivative vector of **e'e** is -2**X'e**. (The normal equations.) The second derivative matrix is $\partial^2(\mathbf{e'e})/\partial \mathbf{b}\partial \mathbf{b'} = 2\mathbf{X'X}$. We need to show that this matrix is positive definite. The diagonal elements are 2n and $2\sum_{i=1}^n x_i^2$ which are clearly both positive. The determinant is

 $[(2n)(2\sum_{i=1}^{n}x_{i}^{2})] - (2\sum_{i=1}^{n}x_{i})^{2} = 4n\sum_{i=1}^{n}x_{i}^{2} - 4(n\overline{x})^{2} = 4n[(\sum_{i=1}^{n}x_{i}^{2}) - n\overline{x}^{2}] = 4n[(\sum_{i=1}^{n}(x_{i} - \overline{x})^{2}].$ Note that a much simpler proof appears after (3-6).

2. Write \mathbf{c} as $\mathbf{b} + (\mathbf{c} - \mathbf{b})$. Then, the sum of squared residuals based on \mathbf{c} is $(\mathbf{y} - \mathbf{X}\mathbf{c})'(\mathbf{y} - \mathbf{X}\mathbf{c}) = [\mathbf{y} - \mathbf{X}(\mathbf{b} + (\mathbf{c} - \mathbf{b}))] '[\mathbf{y} - \mathbf{X}(\mathbf{b} + (\mathbf{c} - \mathbf{b}))] = [(\mathbf{y} - \mathbf{X}\mathbf{b}) + \mathbf{X}(\mathbf{c} - \mathbf{b})] '[(\mathbf{y} - \mathbf{X}\mathbf{b}) + \mathbf{X}(\mathbf{c} - \mathbf{b})]$ $= (\mathbf{y} - \mathbf{X}\mathbf{b}) '(\mathbf{y} - \mathbf{X}\mathbf{b}) + (\mathbf{c} - \mathbf{b}) '\mathbf{X}'\mathbf{X}(\mathbf{c} - \mathbf{b}) + 2(\mathbf{c} - \mathbf{b}) '\mathbf{X}'(\mathbf{y} - \mathbf{X}\mathbf{b}).$ But, the third term is zero, as $2(\mathbf{c} - \mathbf{b}) '\mathbf{X}'(\mathbf{y} - \mathbf{X}\mathbf{b}) = 2(\mathbf{c} - \mathbf{b})\mathbf{X}'\mathbf{e} = \mathbf{0}$. Therefore, $(\mathbf{y} - \mathbf{X}\mathbf{c}) '(\mathbf{y} - \mathbf{X}\mathbf{c}) = \mathbf{e}'\mathbf{e} + (\mathbf{c} - \mathbf{b}) '\mathbf{X}'\mathbf{X}(\mathbf{c} - \mathbf{b})$

 $(\mathbf{y} - \mathbf{X}\mathbf{c})'(\mathbf{y} - \mathbf{X}\mathbf{c}) - \mathbf{e'}\mathbf{e} = (\mathbf{c} - \mathbf{b})'\mathbf{X'}\mathbf{X}(\mathbf{c} - \mathbf{b}).$

The right hand side can be written as $\mathbf{d'd}$ where $\mathbf{d} = \mathbf{X}(\mathbf{c} - \mathbf{b})$, so it is necessarily positive. This confirms what we knew at the outset, least squares is least squares.

3. In the regression of **y** on **i** and **X**, the coefficients on **X** are $\mathbf{b} = (\mathbf{X'M^0X})^{-1}\mathbf{X'M^0y}$. $\mathbf{M}^0 = \mathbf{I} \cdot \mathbf{i}(\mathbf{i'}\mathbf{i})^{-1}\mathbf{i'}$ is the matrix which transforms observations into deviations from their column means. Since \mathbf{M}^0 is idempotent and symmetric we may also write the preceding as $[(\mathbf{X'M^{0\prime}})(\mathbf{M}^0\mathbf{X})]^{-1}(\mathbf{X'M^{0\prime\prime}})(\mathbf{M}^0\mathbf{y})$ which implies that the regression of $\mathbf{M}^0\mathbf{y}$ on $\mathbf{M}^0\mathbf{X}$ produces the least squares slopes. If only **X** is transformed to deviations, we would compute $[(\mathbf{X'M^{0\prime}})(\mathbf{M}^0\mathbf{X})]^{-1}(\mathbf{X'M^{0\prime\prime}})\mathbf{y}$ but, of course, this is identical. However, if only **y** is transformed, the result is $(\mathbf{X'X})^{-1}\mathbf{X'M^{0\prime}}\mathbf{y}$ which is likely to be quite different.

4. What is the result of the matrix product M_1M where M_1 is defined in (3-19) and M is defined in (3-14)?

$$\mathbf{M}_{1}\mathbf{M} = (\mathbf{I} - \mathbf{X}_{1}(\mathbf{X}_{1}'\mathbf{X}_{1})^{-1}\mathbf{X}_{1}')(\mathbf{I} - \mathbf{X}(\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}') = \mathbf{M} - \mathbf{X}_{1}(\mathbf{X}_{1}'\mathbf{X}_{1})^{-1}\mathbf{X}_{1}'\mathbf{M}$$

There is no need to multiply out the second term. Each column of \mathbf{MX}_1 is the vector of residuals in the regression of the corresponding column of \mathbf{X}_1 on all of the columns in \mathbf{X} . Since that \mathbf{x} is one of the columns in \mathbf{X} , this regression provides a perfect fit, so the residuals are zero. Thus, \mathbf{MX}_1 is a matrix of zeroes which implies that $\mathbf{M}_1\mathbf{M} = \mathbf{M}$.

5. The original **X** matrix has *n* rows. We add an additional row, $\mathbf{x}_{s'}$. The new **y** vector likewise has an additional element. Thus, $\mathbf{X}_{n,s} = \begin{bmatrix} \mathbf{X}_n \\ \mathbf{x}'_s \end{bmatrix}$ and $\mathbf{y}_{n,s} = \begin{bmatrix} \mathbf{y}_n \\ y_s \end{bmatrix}$. The new coefficient vector is $\mathbf{b}_{n,s} = (\mathbf{X}_{n,s'} \mathbf{X}_{n,s})^{-1} (\mathbf{X}_{n,s'} \mathbf{y}_{n,s})$. The matrix is $\mathbf{X}_{n,s'} \mathbf{X}_{n,s} = \mathbf{X}_n' \mathbf{X}_n + \mathbf{x}_s \mathbf{x}_s'$. To invert this, use (A -66);

$$(\mathbf{X}'_{n,s}\mathbf{X}_{n,s})^{-1} = (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1} - \frac{1}{1 + \mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}} (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}.$$
 The vector is

$$(\mathbf{X}_{n,s}'\mathbf{y}_{n,s}) = (\mathbf{X}_{n}'\mathbf{y}_{n}) + \mathbf{x}_{s}\mathbf{y}_{s}.$$
 Multiply out the four terms to get

$$(\mathbf{X}_{n,s}'\mathbf{X}_{n,s})^{-1}(\mathbf{X}_{n,s}'\mathbf{y}_{n,s}) =$$

$$\mathbf{b}_{n} - \frac{1}{1 + \mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}} (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{x}'_{s}\mathbf{b}_{n} + (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{y}_{s} - \frac{1}{1 + \mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}} (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{y}_{s} - \frac{1}{1 + \mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}} (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{y}_{s} - \frac{1}{1 + \mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}} (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{x}'_{s}\mathbf{b}_{n}$$

$$\mathbf{b}_{n} + \left[1 - \frac{\mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}}{1 + \mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}}\right] (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{y}_{s} - \frac{1}{1 + \mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}} (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{x}'_{s}\mathbf{b}_{n}$$

$$\mathbf{b}_{n} + \frac{1}{1 + \mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}} (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{y}_{s} - \frac{1}{1 + \mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}\mathbf{x}'_{s}\mathbf{b}_{n}$$

$$\mathbf{b}_{n} + \frac{1}{1 + \mathbf{x}'_{s}(\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}} (\mathbf{X}'_{n}\mathbf{X}_{n})^{-1}\mathbf{x}_{s}(\mathbf{y}_{s}-\mathbf{x}'_{s}\mathbf{b}_{n})$$

6. Define the data matrix as follows: $\mathbf{X} = \begin{bmatrix} \mathbf{i} & \mathbf{x} & \mathbf{0} \\ 1 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \mathbf{X}_1, \mathbf{0} \\ 1 \end{bmatrix} = \begin{bmatrix} \mathbf{X}_1 & \mathbf{X}_2 \end{bmatrix}$ and $\mathbf{y} = \begin{bmatrix} \mathbf{y}_0 \\ y_m \end{bmatrix}$. (The subscripts on the parts of \mathbf{y} refer to the "observed" and "missing" rows of \mathbf{X} . We will use Frish Wough to obtain the first

the parts of **y** refer to the "observed" and "missing" rows of **X**. We will use Frish-Waugh to obtain the first two columns of the least squares coefficient vector. $\mathbf{b}_1 = (\mathbf{X}_1'\mathbf{M}_2\mathbf{X}_1)^{-1}(\mathbf{X}_1'\mathbf{M}_2\mathbf{y})$. Multiplying it out, we find that $\mathbf{M}_2 =$ an identity matrix save for the last diagonal element that is equal to 0.

 $\mathbf{X}_{1}'\mathbf{M}_{2}\mathbf{X}_{1} = \mathbf{X}_{1}'\mathbf{X}_{1} - \mathbf{X}_{1}'\begin{bmatrix}\mathbf{0} & \mathbf{0}\\\mathbf{0}' & 1\end{bmatrix}\mathbf{X}_{1}.$ This just drops the last observation. $\mathbf{X}_{1}'\mathbf{M}_{2}\mathbf{y}$ is computed likewise. Thus,

the coefficients on the first two columns are the same as if y_0 had been linearly regressed on X_1 . The denomonator of R^2 is different for the two cases (drop the observation or keep it with zero fill and the dummy variable). For the first strategy, the mean of the *n*-1 observations should be different from the mean of the full *n* unless the last observation happens to equal the mean of the first *n*-1.

For the second strategy, replacing the missing value with the mean of the other n-1 observations, we can deduce the new slope vector logically. Using Frisch-Waugh, we can replace the column of x's with deviations from the means, which then turns the last observation to zero. Thus, once again, the coefficient on the x equals what it is using the earlier strategy. The constant term will be the same as well.

7. For convenience, reorder the variables so that $\mathbf{X} = [\mathbf{i}, \mathbf{P}_d, \mathbf{P}_n, \mathbf{P}_s, \mathbf{Y}]$. The three dependent variables are \mathbf{E}_d , \mathbf{E}_n , and \mathbf{E}_s , and $\mathbf{Y} = \mathbf{E}_d + \mathbf{E}_n + \mathbf{E}_s$. The coefficient vectors are

$$\mathbf{b}_d = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{E}_d,$$

$$\mathbf{b}_n = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{E}_n, \text{ and }$$

$$\mathbf{b}_s = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{E}_s.$$

The sum of the three vectors is

$$\mathbf{b} = (\mathbf{X'X})^{-1}\mathbf{X'}[\mathbf{E}_d + \mathbf{E}_n + \mathbf{E}_s] = (\mathbf{X'X})^{-1}\mathbf{X'Y}.$$

Now, **Y** is the last column of **X**, so the preceding sum is the vector of least squares coefficients in the regression of the last column of **X** on all of the columns of **X**, including the last. Of course, we get a perfect fit. In addition, $\mathbf{X'}[\mathbf{E}_d + \mathbf{E}_n + \mathbf{E}_s]$ is the last column of $\mathbf{X'X}$, so the matrix product is equal to the last column of an identity matrix. Thus, the sum of the coefficients on all variables except income is 0, while that on income is 1.

8. Let \overline{R}_{K}^{2} denote the adjusted R^{2} in the full regression on *K* variables including \mathbf{x}_{k} , and let \overline{R}_{1}^{2} denote the adjusted R^{2} in the short regression on *K*-1 variables when \mathbf{x}_{k} is omitted. Let R_{K}^{2} and R_{1}^{2} denote their unadjusted counterparts. Then,

$$R_K^2 = 1 - \mathbf{e'e/y'M^0y}$$

$$R_1^2 = 1 - \mathbf{e_1'e_1/y'M^0y}$$

where **e'e** is the sum of squared residuals in the full regression, $\mathbf{e}_1'\mathbf{e}_1$ is the (larger) sum of squared residuals in the regression which omits \mathbf{x}_k , and $\mathbf{y'}\mathbf{M}^0\mathbf{y} = \sum_i (y_i - \overline{y})^2$.

Then, and

 $\overline{R}_1^2 = 1 - [(n-1)/(n-(K-1))](1-R_1^2).$

 $\overline{R}_{K}^{2} = 1 - [(n-1)/(n-K)](1 - R_{K}^{2})$

The difference is the change in the adjusted R^2 when \mathbf{x}_k is added to the regression,

 $\overline{R}_{K}^{2} - \overline{R}_{1}^{2} = [(n-1)/(n-K+1)][\mathbf{e}_{1}'\mathbf{e}_{1}/\mathbf{y'M}^{0}\mathbf{y}] - [(n-1)/(n-K)][\mathbf{e'e}/\mathbf{y'M}^{0}\mathbf{y}].$

The difference is positive if and only if the ratio is greater than 1. After cancelling terms, we require for the adjusted R^2 to increase that $\mathbf{e_1'e_1}/(n\cdot K+1)]/[(n\cdot K)/\mathbf{e'e}] > 1$. From the previous problem, we have that $\mathbf{e_1'e_1} = \mathbf{e'e} + b_K^2(\mathbf{x}_k'\mathbf{M}_1\mathbf{x}_k)$, where \mathbf{M}_1 is defined above and b_k is the least squares coefficient in the full regression of \mathbf{y} on \mathbf{X}_1 and \mathbf{x}_k . Making the substitution, we require $[(\mathbf{e'e} + b_K^2(\mathbf{x}_k'\mathbf{M}_1\mathbf{x}_k))(n\cdot K)]/[(n\cdot K)\mathbf{e'e} + \mathbf{e'e}] > 1$. Since $\mathbf{e'e} = (n\cdot K)s^2$, this simplifies to $[\mathbf{e'e} + b_K^2(\mathbf{x}_k'\mathbf{M}_1\mathbf{x}_k)]/[\mathbf{e'e} + s^2] > 1$. Since all terms are positive, the fraction is greater than one if and only $b_K^2(\mathbf{x}_k'\mathbf{M}_1\mathbf{x}_k) > s^2$ or $b_K^2(\mathbf{x}_k'\mathbf{M}_1\mathbf{x}_k/s^2) > 1$. The denominator is the estimated variance of b_k , so the result is proved.

9. This R^2 must be lower. The sum of squares associated with the coefficient vector which omits the constant term must be higher than the one which includes it. We can write the coefficient vector in the regression without a constant as $\mathbf{c} = (0, \mathbf{b}^*)$ where $\mathbf{b}^* = (\mathbf{W'W})^{-1}\mathbf{W'y}$, with \mathbf{W} being the other *K*-1 columns of \mathbf{X} . Then, the result of the previous exercise applies directly.

10. We use the notation 'Var[.]' and 'Cov[.]' to indicate the sample variances and covariances. Our information is Var[N] = 1, Var[D] = 1, Var[P] = 1. Since C = N + D, Var[C] = Var[N] + Var[D] + 2Cov[N,D] = 2(1 + Cov[N,D]).

From the regressions, we have

	$\operatorname{Cov}[C,Y]/\operatorname{Var}[Y] = \operatorname{Cov}[C,Y] = .8.$
But,	$\operatorname{Cov}[C,Y] = \operatorname{Cov}[N,Y] + \operatorname{Cov}[D,Y].$
Also,	$\operatorname{Cov}[C,N]/\operatorname{Var}[N] = \operatorname{Cov}[C,N] = .5,$
but,	Cov[C,N] = Var[N] + Cov[N,D] = 1 + Cov[N,D], so Cov[N,D] =5,
so that	Var[C] = 2(1 +5) = 1.
And,	$\operatorname{Cov}[D,Y]/\operatorname{Var}[Y] = \operatorname{Cov}[D,Y] = .4.$
Since	Cov[C,Y] = .8 = Cov[N,Y] + Cov[D,Y], Cov[N,Y] = .4.
Finally,	Cov[C,D] = Cov[N,D] + Var[D] =5 + 1 = .5.
Now in the regression of	f C on D the sum of squared residuals is $(r, 1)[Var[C] - (Cav[CD]/Var[D)]$

Now, in the regression of *C* on *D*, the sum of squared residuals is $(n-1){\text{Var}[C] - (\text{Cov}[C,D]/\text{Var}[D])^2\text{Var}[D]}$ based on the general regression result $\Sigma e^2 = \Sigma(y_i - \overline{y})^2 - b^2\Sigma(x_i - \overline{x})^2$. All of the necessary figures were obtained above. Inserting these and n-1 = 20 produces a sum of squared residuals of 15.

11.	Computed results are
Reg	ess;lhs=realinv;rhs=one,realgnp,interest\$

Ordinary	lost squares regres	sion			
Orurnary	reast squares regres	31011			
LHS=REALINV	Mean	=	2.42007		
	Standard deviation	=	.26267		
	No. of observations	=	15	DegFreedom	Mean square
Regression	Sum of Squares	=	.521605	2	.26080
Residual	Sum of Squares	=	.444305	12	.03703
Total	Sum of Squares	=	.965911	14	.06899
	Standard error of e	=	.19242	Root MSE	.17211

Fit Model tes	R-squared st F[2, 1	.2] =	.54 7.04	4001 4388	R-bar square Prob F > F*	d .46335 .00947
+ REALINV	Coefficient	Standard Error	t	Prob. t >T*	95% Co Int	nfidence erval
Constant REALGNP INTEREST	04298 .01945** .10448***	.86319 .00786 .02842	05 2.47 3.68	.9611 .0293 .0032	-1.92371 .00232 .04256	1.83775 .03657 .16640
+ Namelist; Matrix ; RESULT	X=one,realgnp, list ; x'x ; x' 1	interest\$ realinv\$ 2		3		
1 2 3 RESULT	15.0000 1491.20 76.0600 1	1491.20 149038. 7453.03	76. 745 446	.0600 53.03 5.323		
1 2 3 Matrix ; RESULT	36.3010 3612.90 188.300 list ; <x'x>*x' 1</x'x>	realinv\$				
+ 1 2 3 Matrix ; BA	0429785 .0194467 .104480 list ; ba= <x'x> 1</x'x>	**x'realinv\$				
1 2 3 Matrix ; Calc ; [CALC] R2	0429785 .0194467 .104480 e = realinv - x list ; r2 = 1 - 2 =	*ba\$ · e'e / ((n-1)* .5400140	'var(reali	inv))	\$	

12. The results cannot be correct. Since $\log S/N = \log S/Y + \log Y/N$ by simple, exact algebra, the same result must apply to the least squares regression results. That means that the second equation estimated must equal the first one plus log *Y/N*. Looking at the equations, that means that all of the coefficients would have to be identical save for the second, which would have to equal its counterpart in the first equation, plus 1. Therefore, the results cannot be correct. In an exchange between Leff and Arthur Goldberger that appeared later in the same journal, Leff argued that the difference was simple rounding error. You can see that the results in the second equation resemble those in the first, but not enough so that the explanation is credible. Further discussion about the data themselves appeared in subsequent discussion. [See Goldberger (1973) and Leff (1973).]

13. a. Consider a regression of y on x_1 , x_2 and x3. The incremental contribution of x_3 will be different depending on whether the order entered is (x_1,x_3,x_2) or (x_1,x_2,x_3) , (x_2,x_1,x_3) , or (x_2,x_3,x_1) .

b. Use the equation above (3-31) and consider x_2 after x_1 . If x_1 and x_2 are orthogonal, then $\mathbf{X}_2'\mathbf{M}_1\mathbf{X}_2 = \mathbf{X}_2'\mathbf{X}_2$ and the result reduces to $R_{1,2}^2 = R_1^2 + R_2^2$. This is the if part. For only if, note that (3-31) implies that if the variables are not orthogonal, then, as observed earlier the previous result cannot hold.

c. Entering T first raises R² from 0.00000 to 0.01090. Entering T last raises R² from .54013 to .78776.

01	rdinary	lea	ast squares	regression	
т	entered	first	R-squared	=	.01090
т	not ente	ered	R-squared	=	.54013
т	entered	last	R-squared	=	.78776

Application

```
?_____
? Chapter 3 Application 1
2_____
Read $
(Data appear in the text.)
Namelist ; X1 = one,educ,exp,ability$
Namelist ; X2 = mothered, fathered, sibs$
?_____
? a.
?-----
Regress ; Lhs = wage ; Rhs = x1$
+-----+
| Ordinary least squares regression
| LHS=WAGE Mean
               = 2.059333
         Standard deviation = .2583869
| WTS=none
                            15
          Number of observs. =
         Parameters
Degrees of freedom = 11
.7633163
| Model size Parameters
| Residuals Sum of squares
         Standard error of e =
                           .2634244
         R-squared = .1833511
| Fit
         Adjusted R-squared = -.3937136E-01 |
| Model test F[ 3, 11] (prob) = .82 (.5080) |
|Variable| Coefficient | Standard Error |t-ratio |P[|T|>t]| Mean of X|
Constant| 1.66364000 .61855318 2.690 .0210
        .01453897.04902149.297.772312.8666667.07103002.048034151.479.16732.8000000.02661537.09911731.269.7933.36600000
EDUC |
      1
EXP
ABILITY |
?_____
?h.
?_____
Regress ; Lhs = wage ; Rhs = x1, x2$
+-----+
| Ordinary least squares regression
                        = 2.059333
| LHS=WAGE
        Mean
         Standard deviation = .2583869
                          15
7
8
| WTS=none Number of observs. =
| Model size Parameters
                       =
Degrees of freedom=8ResidualsSum of squares=.4522662
          Standard error of e =
                           .2377673
R-squared
                           .5161341
                        =
| Fit
          Adjusted R-squared =
                           .1532347
| Model test F[ 6, 8] (prob) =
                           1.42 (.3140) |
+-----
                 _____+
     __+____+
|Variable| Coefficient | Standard Error |t-ratio |P[|T|>t]| Mean of X|
Constant|.04899633.94880761.052.9601EDUC |.02582213.04468592.578.579312.8666667EXP |.10339125.047345412.184.06052.80000000ABILITY |.03074355.12120133.254.8062.36600000MOTHERED |.10163069.070175021.448.185612.0666667FATHERED |.00164437.04464910.037.971512.6666667SIBS |.05916922.06901801.857.41622.2000000
?------
```

? c.

```
Regress ; Lhs = mothered ; Rhs = x1 ; Res = meds $
Regress ; Lhs = fathered ; Rhs = x1 ; Res = feds $
Regress ; Lhs = sibs ; Rhs = x1 ; Res = sibss $
Namelist ; X2S = meds,feds,sibss $
Matrix ; list ; Mean(X2S) $
Matrix Result has 3 rows and 1 columns.
           1
      +----
     1| -.1184238D-14
     2| .1657933D-14
     3| -.5921189D-16
The means are (essentially) zero. The sums must be zero, as these new
variables are orthogonal to the columns of X1. The first column in X1 is a
column of ones, so this means that these residuals must sum to zero.
? d.
?_____
Namelist ; X = X1, X2 $
Matrix ; i = init(n,1,1) $
Matrix ; M0 = iden(n) - 1/n*i*i' $
Matrix ; b12 = <X'X>*X'wage$
Calc ; list ; ym0y = (N-1)*var(wage) $
Matrix ; list ; cod = 1/ym0y * b12'*X'*M0*X*b12 $
Matrix COD has 1 rows and 1 columns.
           1
      +-----
     1| .51613
Matrix ; e = wage - X*b12 $
      ; list ; cod = 1 - 1/ym0y * e'e $
Calc
      = .516134
COD
The R squared is the same using either method of computation.
Calc ; list ; RsqAd = 1 - (n-1)/(n-col(x))*(1-cod)$
RSQAD = .153235
? Now drop the constant
Namelist ; X0 = educ,exp,ability,X2 $
Matrix ; i = init(n,1,1) $
Matrix ; M0 = iden(n) - 1/n*i*i' $
Matrix ; b120 = <X0'X0>*X0'wage$
Matrix ; list ; cod = 1/ym0y * b120'*X0'*M0*X0*b120 $
Matrix COD has 1 rows and 1 columns.
           1
      +-----
     1| .52953
Matrix ; e0 = wage - X0*b120 $
Calc ; list ; cod = 1 - 1/ym0y * e0'e0 $
           .515973
COD
      =
The R squared now changes depending on how it is computed. It also goes up,
completely artificially.
?-----
? e.
?------
The R squared for the full regression appears immediately below.
? f.
Regress ; Lhs = wage ; Rhs = X1,X2 $
+----+
| Ordinary least squares regression
| WTS=none Number of observs. =
| Model size Parameters =
                                         1
                                    15
                                7
8
                                          Degrees of freedom =
| Fit
           R-squared = .5161341
+----+
```

Variable	Coefficient	Standard Error	t-ratio	P[T >t]	Mean of X
Constant EDUC EXP ABILITY MOTHERED FATHERED SIBS Ordinary WTS=none Model si Fit 	.04899633 .02582213 .10339125 .03074355 .10163069 .00164437 .05916922 Lhs = wage ; Rk y least squar e Number of ize Parameters Degrees of R-squared Adjusted F	.94880761 .04468592 .04734541 .12120133 .07017502 .04464910 .06901801 hs = X1,X2S \$ res regression observs. = s = f freedom = = R-squared =	.052 .578 2.184 .254 1.448 .037 .857 15 7 8 .5161341 .1532347	++ .9601 .5793 .0605 .8062 .1856 .9715 .4162	12.8666667 2.8000000 .36600000 12.0666667 12.6666667 2.20000000
Variable	Coefficient	Standard Error	t-ratio	++ P[T >t]	Mean of X
Constant EDUC EXP ABILITY MEDS FEDS SIBSS	1.66364000 .01453897 .07103002 .02661537 .10163069 .00164437 .05916922	.55830716 .04424689 .04335571 .08946345 .07017502 .04464910 .06901801	2.980 .329 1.638 .297 1.448 .037 .857	.0176 .7509 .1400 .7737 .1856 - .9715 .4162 -	12.8666667 2.8000000 .36600000 .118424D-14 .165793D-14 .592119D-16

In the first set of results, the first coefficient vector is

 $\mathbf{b}_1 = (\mathbf{X}_1'\mathbf{M}_2\mathbf{X}_1)^{-1}\mathbf{X}_1'\mathbf{M}_2\mathbf{y}$ and $\mathbf{b}_2 = (\mathbf{X}_2'\mathbf{M}_1\mathbf{X}_2)^{-1}\mathbf{X}_2'\mathbf{M}_1\mathbf{y}$

In the second regression, the second set of regressors is M_1X_2 , so

 $\mathbf{b}_1 = (\mathbf{X}_1'\mathbf{M}_{12} \mathbf{X}_1)^{-1} \mathbf{X}_1'\mathbf{M}_{12} \mathbf{y} \text{ where } \mathbf{M}_{12} = \mathbf{I} - (\mathbf{M}_1 \mathbf{X}_2)[(\mathbf{M}_1 \mathbf{X}_2)'(\mathbf{M}_1 \mathbf{X}_2)]^{-1}(\mathbf{M}_1 \mathbf{X}_2)'$ Thus, because the "M" matrix is different, the coefficient vector is different. The second set of coefficients in the second regression is

 $\mathbf{b}_2 = [(\mathbf{M}_1 \mathbf{X}_2)' \mathbf{M}_1 (\mathbf{M}_1 \mathbf{X}_2)]^{-1} (\mathbf{M}_1 \mathbf{X}_2) \mathbf{M}_1 \mathbf{y} = (\mathbf{X}_2' \mathbf{M}_1 \mathbf{X}_2)^{-1} \mathbf{X}_2' \mathbf{M}_1 \mathbf{y}$ because \mathbf{M}_1 is idempotent.

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